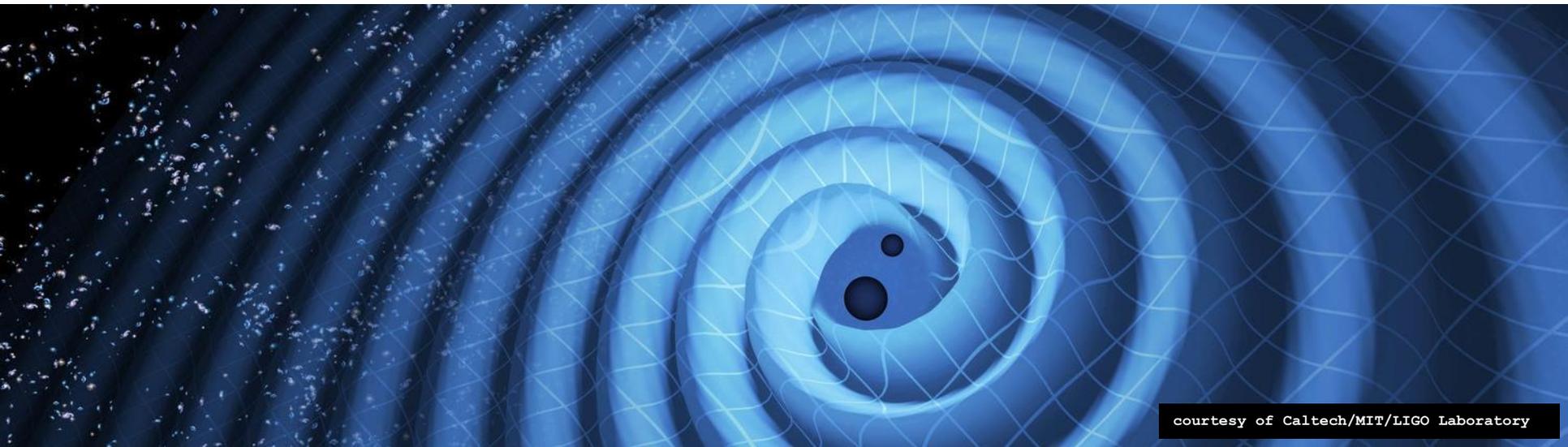


# Detecting Binary Black Hole Mergers through LIGO Gravity Wave Measurements with Ultra96

**AVNET**<sup>®</sup>  
Reach Further™



courtesy of Caltech/MIT/LIGO Laboratory

# Gravity primer

# What is Gravity?

Sir Isaac Newton



$$F = \frac{Gm_1m_2}{r^2}$$



Painting by Sir Godfrey Kneller 1689: <http://www.newton.ac.uk/about/art-artefacts/newton-portrait>

# What are Gravity Waves (GW) ?

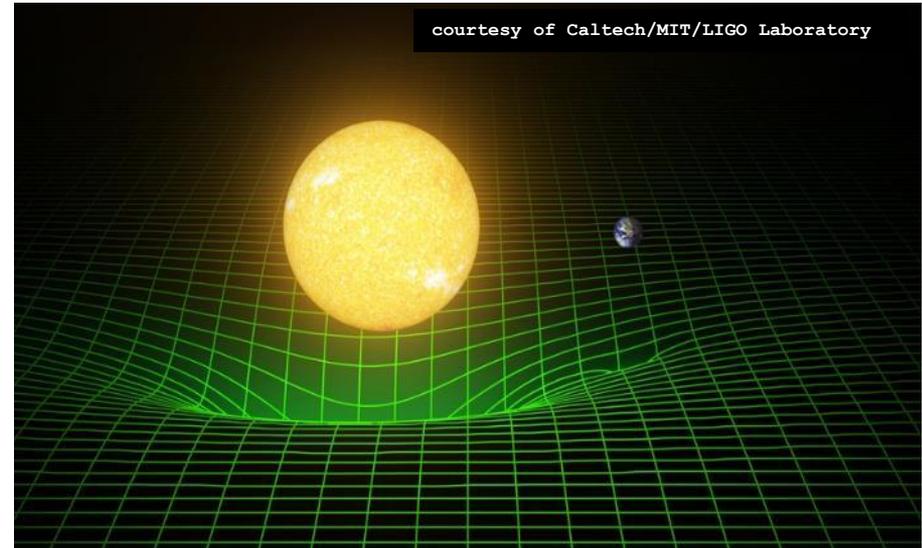
- Einstein said (paraphrased):

$$h_{\mu\nu} \approx \frac{1}{r} \frac{G}{c^4} I_{\mu\nu}$$

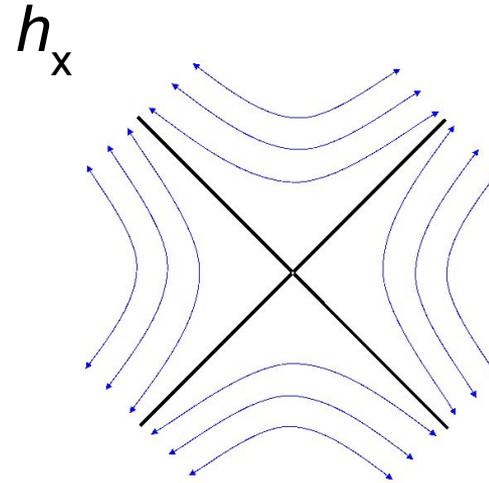
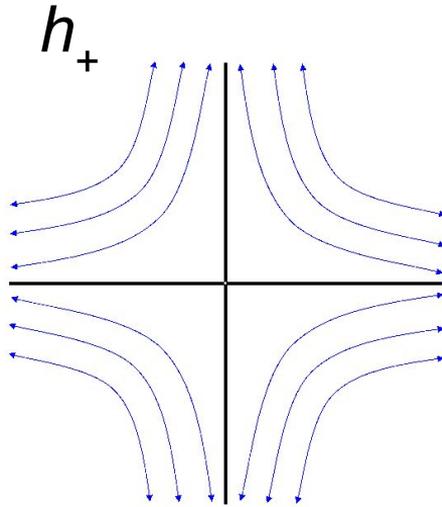
## What if you are not Einstein?

- Just accept that GW are physical ripples in the fabric of space-time ☺

Gravitational waves are *propagating mathematical solutions* to the Field Equations of General Relativity that show space and time are dynamically coupled



# A strain through space and time:



**2 polarizations of *strain***

courtesy of Caltech/MIT/LIGO Laboratory

# The Astrophysical Gravitational-Wave Source Catalog



## Coalescing Binary Systems

- Black hole – black hole
- Black hole – neutron star
- Neutron star – neutron star (modeled waveform)

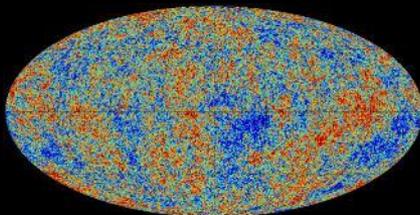
Credit: Bohn, Hébert, Throwe, SXS



## Transient 'Burst' Sources

- asymmetric core collapse supernovae
- cosmic strings
- ??? (Unmodeled waveform)

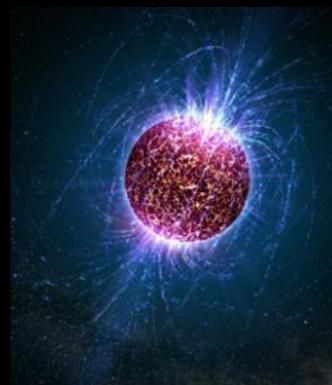
Credit: Chandra X-ray Observatory



## Stochastic Background

- residue of the Big Bang
  - incoherent sum of unresolved 'point' sources
- (stochastic, incoherent noise background)

Credit: Planck Collaboration



## Continuous Sources

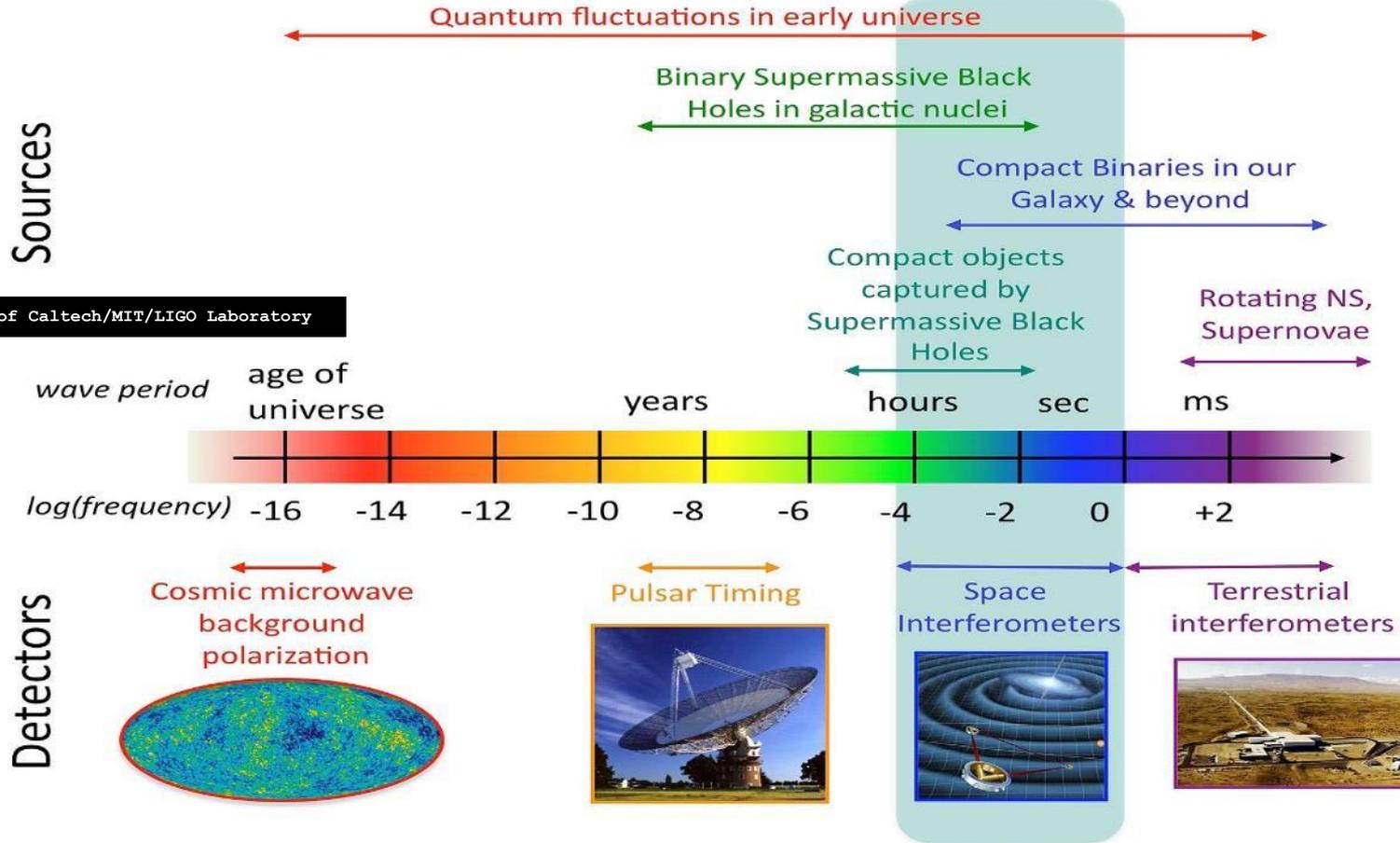
- Spinning neutron stars (monotone waveform)

Credit: Casey Reed, Penn State

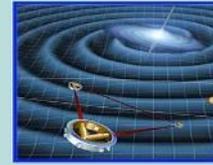
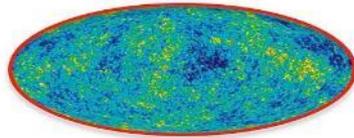
# The Gravitational Wave Spectrum

Sources

courtesy of Caltech/MIT/LIGO Laboratory



Detectors

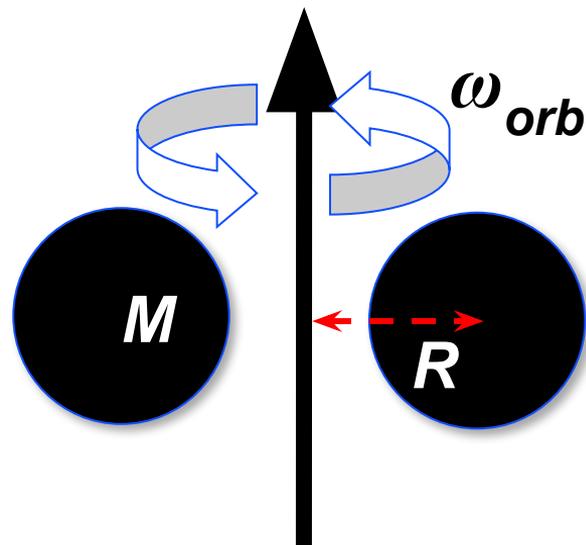


# Gravity waves and binary black holes:

## 10M<sub>⊙</sub> Binary Black Hole System

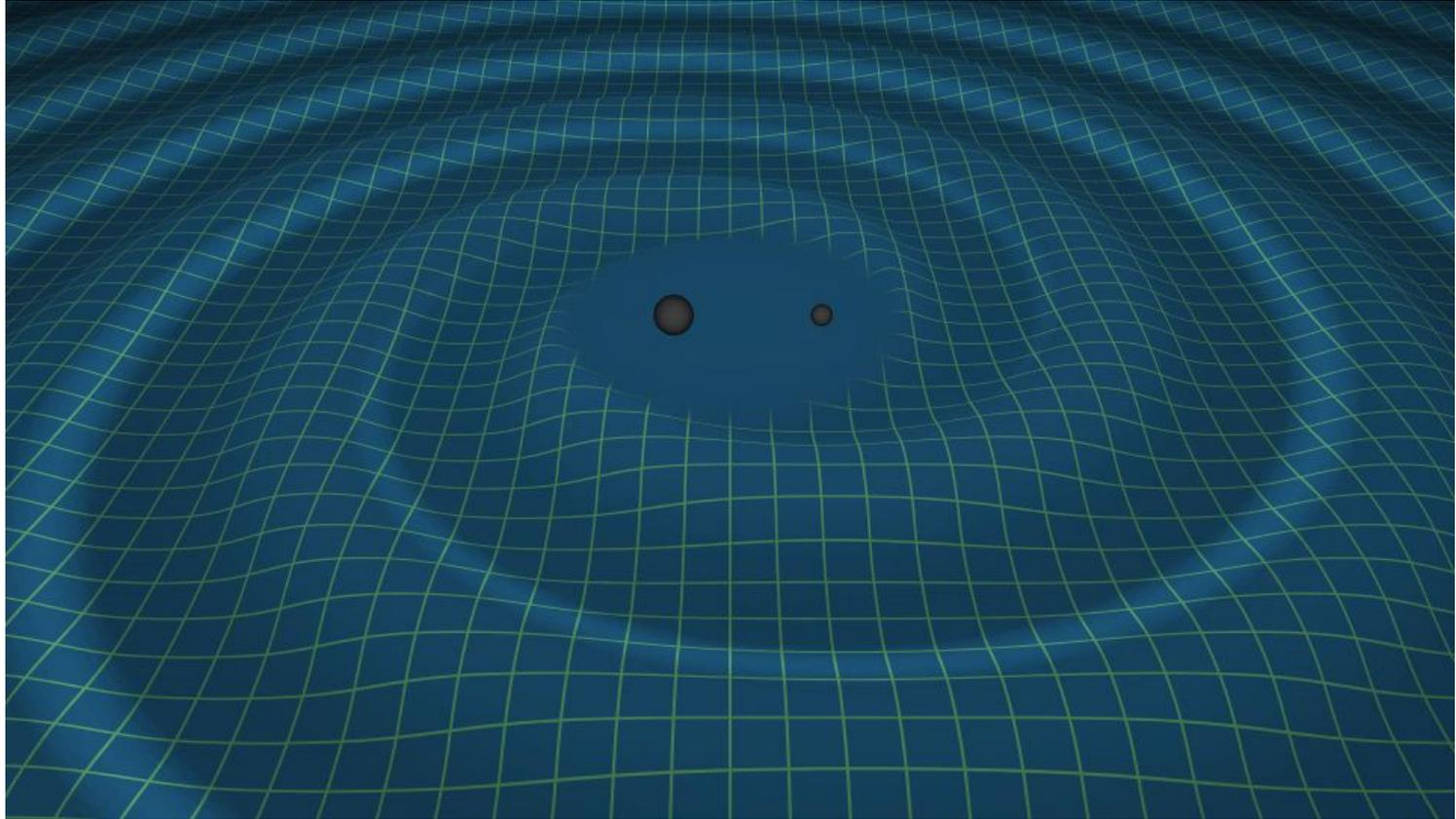
$$h \approx \frac{8GM R^2 \omega_{orb}^2}{rc^4} \sim 10^{-21}$$

Physically,  $h$  (a *strain*):  $\Delta L/L$



courtesy of Caltech/MIT/LIGO Laboratory

# Binary black hole merger simulation:



courtesy of Caltech/MIT/LIGO Laboratory

AVNET

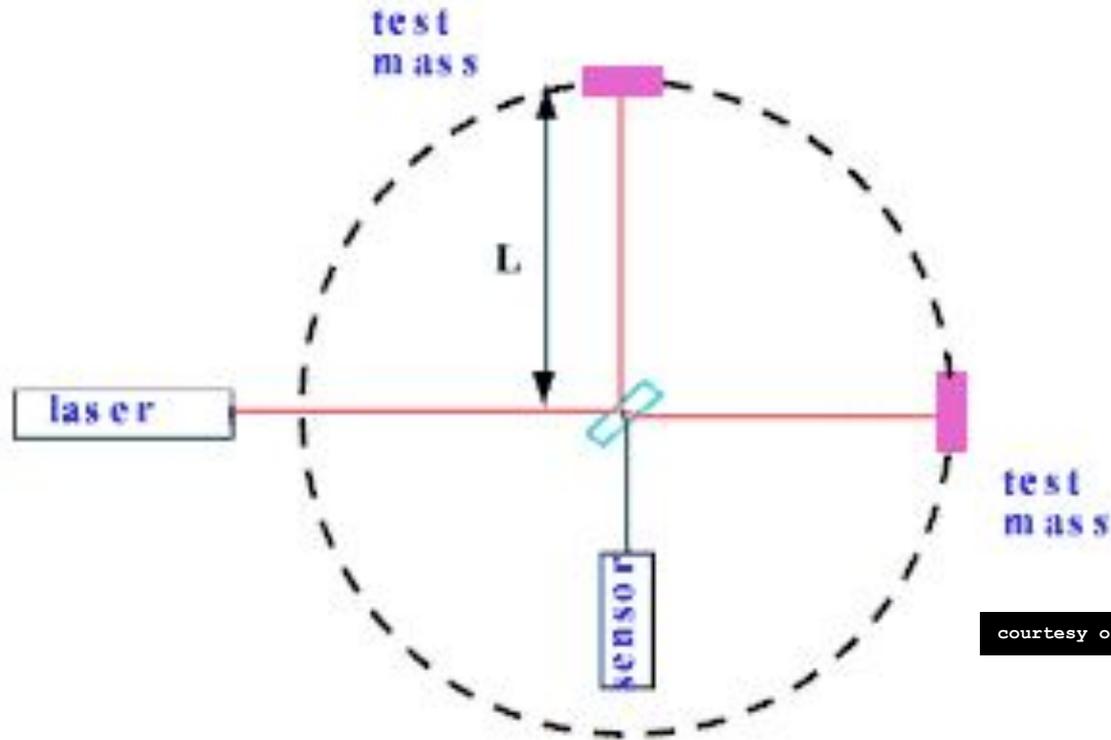
# LIGO and Laser Interferometry

# LIGO = Laser Interferometer Gravitational-wave Observatory:



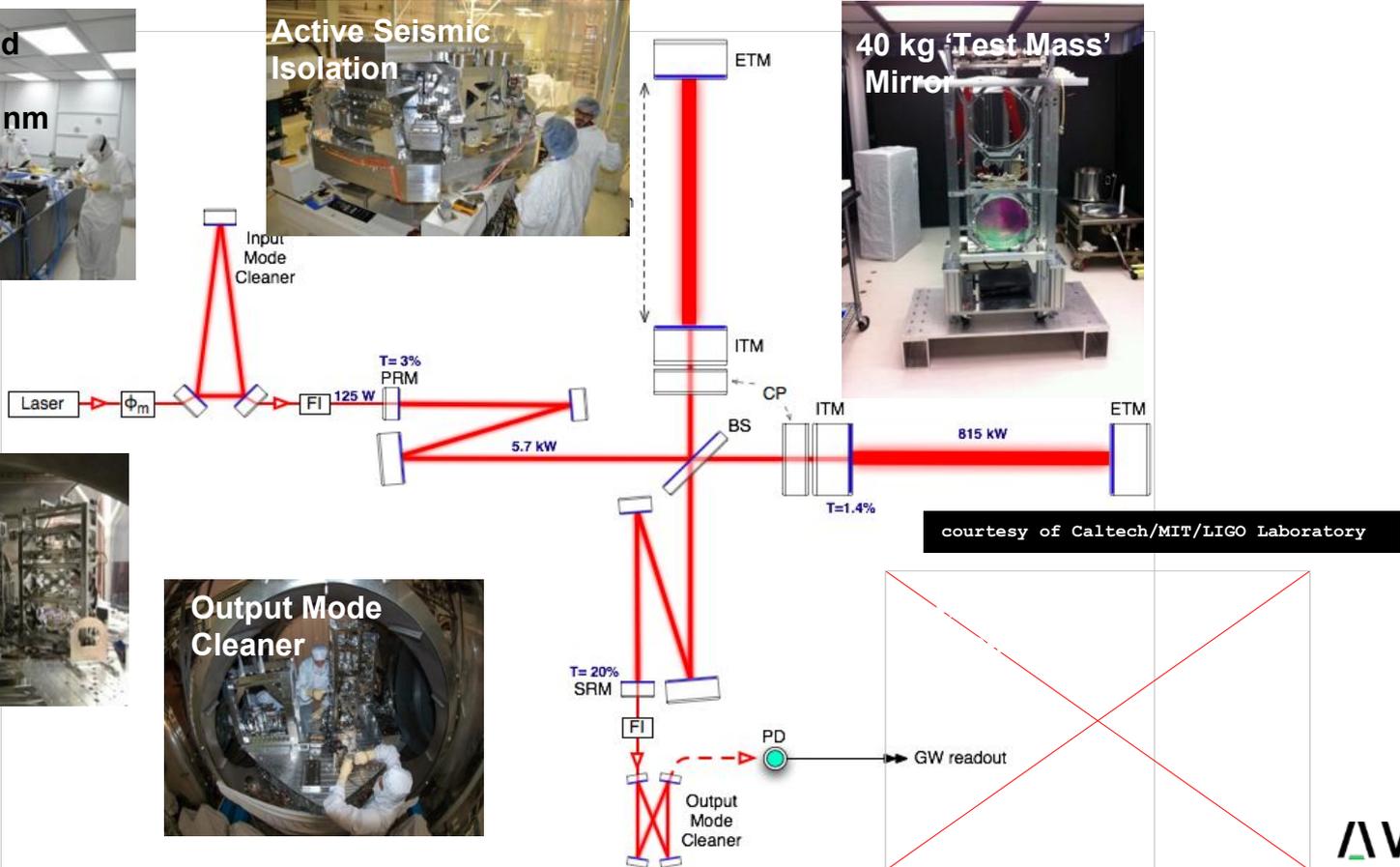
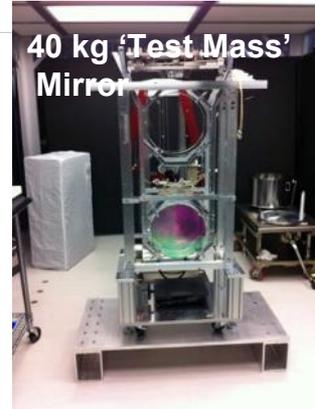
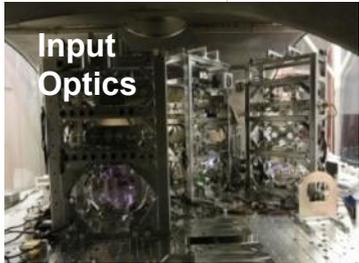
Hansford, Washington  
(Each vacuum tube is ~4km)

# Gravity wave effects on a laser interferometer:



courtesy of Caltech/MIT/LIGO Laboratory

# LIGO = Laser Interferometer Gravitational-wave Observatory:



courtesy of Caltech/MIT/LIGO Laboratory

# Noise floor determines detection limitations (receiver sensitivity):

## Fundamental Noises:

### *I. Displacement Noises*

→  $\Delta L(f)$

- Seismic noise
- Radiation Pressure
- Thermal noise
  - Suspensions
  - Optics

### *II. Sensing Noises*

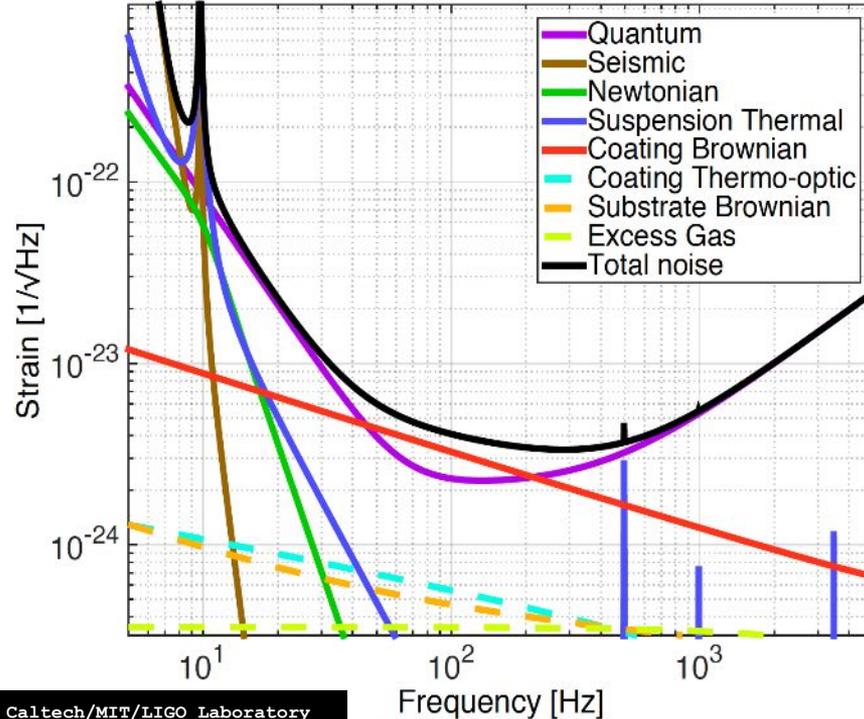
→  $\Delta t_{\text{photon}}(f)$

- Shot Noise
- Residual Gas

## Technical Noises:

→ *Hundreds of them...*

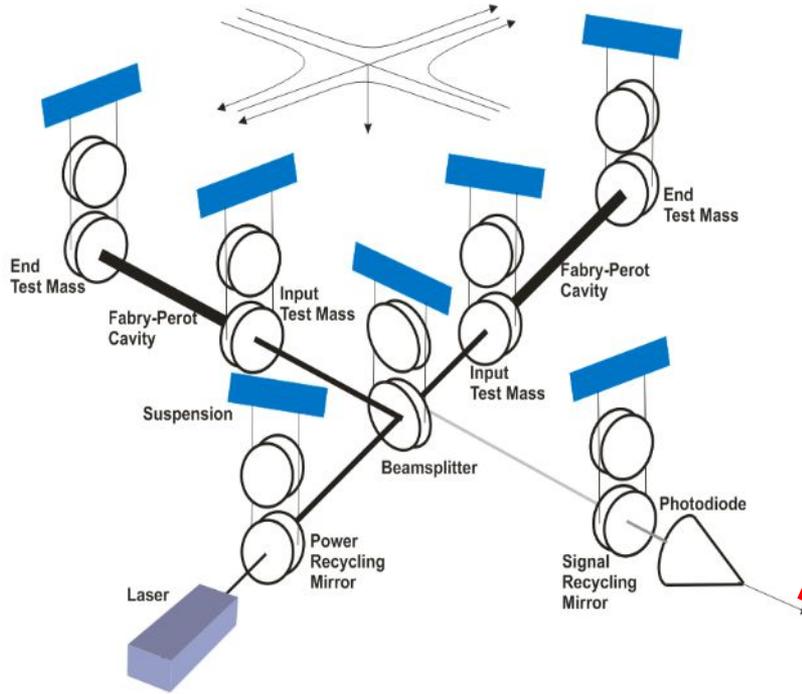
## Advanced LIGO Design



courtesy of Caltech/MIT/LIGO Laboratory

# LIGO signals, data and Event catalog

# LIGO = Laser Interferometer Gravitational-wave Observatory:



courtesy of Caltech/MIT/LIGO Laboratory

**$h(t)$ : 16384 Hz rate**  
**LOSC  $h(t)$ : 4096 Hz rate**

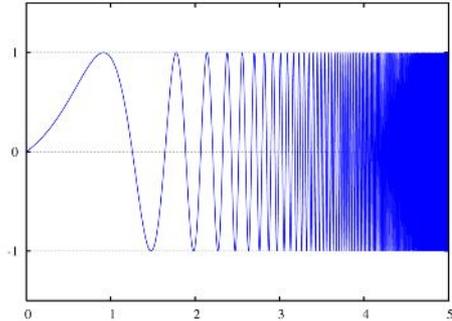
***Saved on the LIGO servers in HDF5 file format***

***Analyzed and processed, GW Events cataloged***

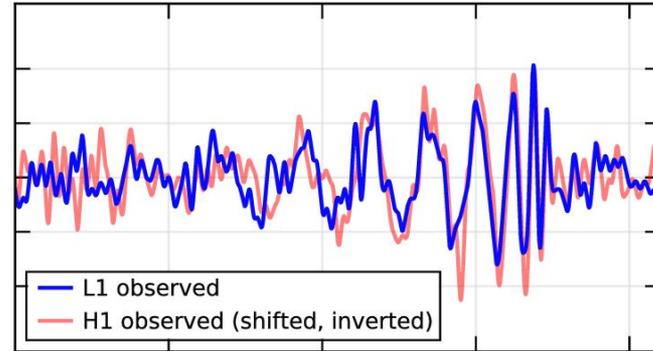
# What signal are they looking for?

After all the signal processing what is the confirming signal for a binary merger: Chirp!

Constant envelope exponential chirp:



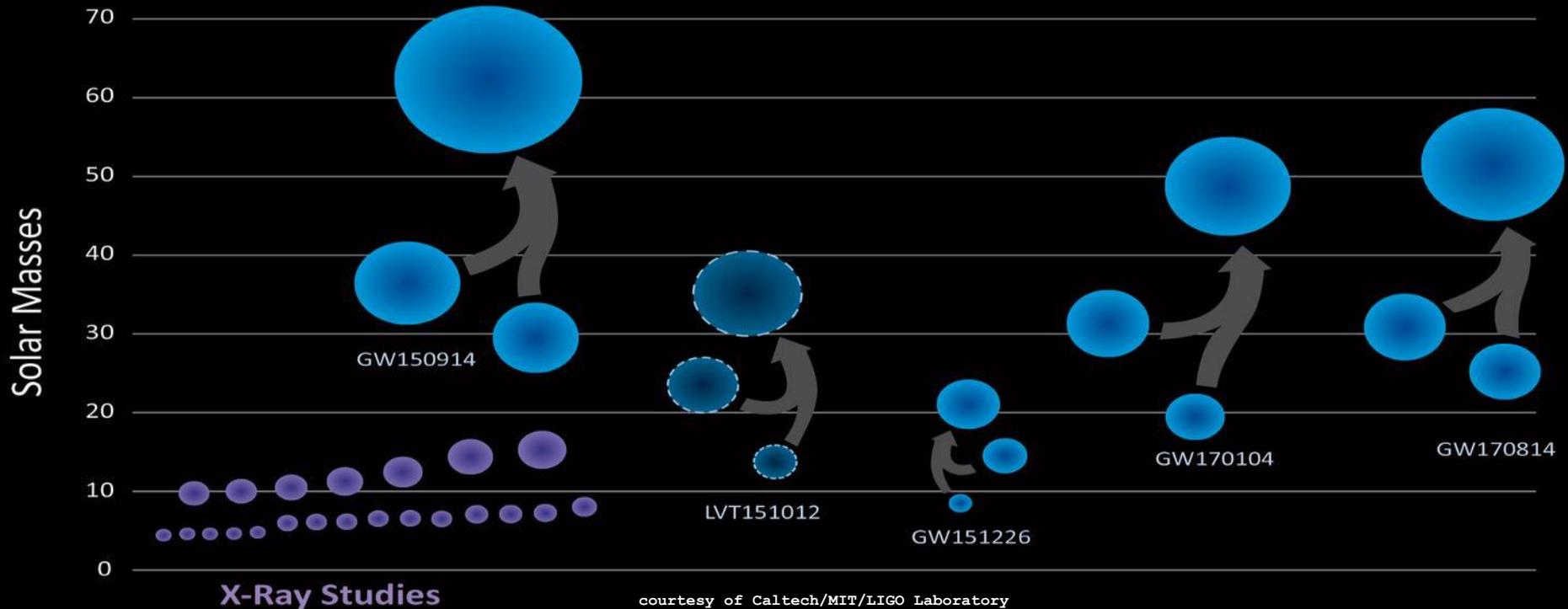
Actual measured strain signal:



courtesy of Caltech/MIT/LIGO Laboratory

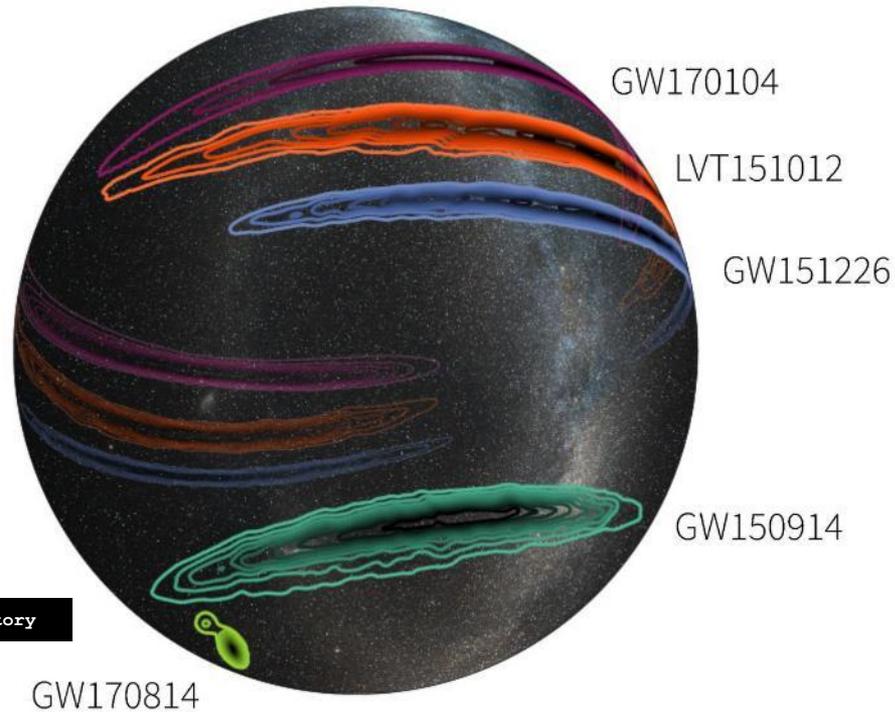


# Black Holes of Known Mass



courtesy of Caltech/MIT/LIGO Laboratory

# Locating the origin using multiple detectors and TDOA:



courtesy of Caltech/MIT/LIGO Laboratory

(Skymap projection onto a sphere  
of detected events as of Sept 2017)

Earth

Space



courtesy of Caltech/MIT/LIGO Laboratory

# Event case study: GW150914

- Black hole masses involved:  $36M_{\odot}$   $\rightarrow$   $29M_{\odot}$   $\rightarrow$   $62M_{\odot}$
- Distance of origin from Earth: over 1 BILLION Light Years
- LIGO's 4km mass movement:
  - Approx. 1000 times less than width of a proton (2e-18 Meters)
  - Proportionally equivalent to changing the distance to the nearest star (Proxima Centauri) 4.3 light years away by one hair's width
- General event notes:
  - LVT = LIGO Virgo Trigger which is a candidate that has not been scrutinized enough to not just be a false alarm
  - Other event examples and details found here: <https://losc.ligo.org/events/>
  - Notation decoder:
    - **GW** = Gravity Wave detected with great certainty (The false alarm rate for this event is statistically estimated to be less than 1 event per 203,000 years)
    - **15** = Year, **09** = Month, **14** = Day

Using Ultra96 for  
gravity wave detection  
and the case for  
PYNQ™

## Accessing LIGO data yourself:

- Data ( <https://losc.ligo.org/data/> )
  - Public
    - Confirmed “events”, some triggers and partial timelines with reliability metrics (mostly 4kHz) from multiple detectors
    - More will be added in the future
    - LIGO members (access to full timeline and 16kHz)
- Easy way is to use Python (or C or Matlab)
  - Use readligo.py ( [https://losc.ligo.org/tutorial\\_gps/](https://losc.ligo.org/tutorial_gps/) )

## Data wisdom:

- Download .hdf5 from the server then easy peasy with readligo.py:  
`strain, time, dq = rl.loaddata('ligo_data/H-H1_LOSC_4_V1-842653696-4096.hdf5', 'H1')`
- Read the instructions! They explain all the strings used above (like 'H1' is Handon, Wa and 'L1' is Livingston, La, etc.)!
- When searching for your own events learn where injection (test) samples are located!
- Use the data quality flags to mask out invalid samples that occur due to system maintenance!
- For a manipulatable example study the Jupyter Notebook!

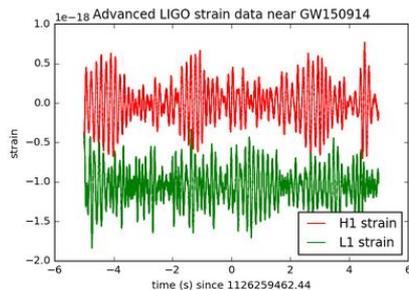
# LIGO Jupyter Notebook for Cataloged Events on Ultra96:

- All notebooks (including for download to run on Ultra96\*): <https://losc.ligo.org/tutorials/>
- Direct link to Notebook in an Azure binder: [https://notebooks.azure.com/losc/libraries/tutorials/html/LOSC\\_Event\\_tutorial.ipynb](https://notebooks.azure.com/losc/libraries/tutorials/html/LOSC_Event_tutorial.ipynb)

```
In [8]: # plot +/- deltat seconds around the event:
# index into the strain time series for this time interval:
deltat = 5
indx = np.where((time >= tevent-deltat) & (time < tevent+deltat))
print(tevent)

if make_plots:
    plt.figure()
    plt.plot(time[indx]-tevent, strain_H1[indx], 'r', label='H1 strain')
    plt.plot(time[indx]-tevent, strain_L1[indx], 'g', label='L1 strain')
    plt.xlabel('time (s) since '+str(tevent))
    plt.ylabel('strain')
    plt.legend(loc='lower right')
    plt.title('Advanced LIGO strain data near '+eventname)
    plt.savefig(eventname+'_'+strain+'_plottype')
```

1126259462.44



Jupyter

PYNQ™

courtesy of Caltech/MIT/LIGO Laboratory

\* Xilinx's PYNQ™ for Ultra96 framework comes with Jupyter installed on the target



AVNET™

# Xilinx PYNQ™ for Ultra96

## ▪What is PYNQ?

An open source software **framework** designed to make Ultra96 more Python friendly and easier for Python to interact with the PL in embedded systems. It is comprised of:

- PetaLinux (aarch64 kernel)
- Ubuntu Bionic root file-system
- Full Python (as opposed to Micro Python)
- Jupyter Notebooks
- Python libraries for using the Xilinx PS and PL



## ▪Why would I want to use it?

In combination with using PL it has the ability to make some of your slow Python programs run FAST, really really FAST and allows Python to control hardware that other platforms could only dream about. It can also dramatically reduce design time and effort!

# When will Xilinx PYNQ™ be available for Ultra96?



- PYNQ for Ultra96 is coming soon, expected 1<sup>st</sup> week of Oct. 2018!!!

<http://www.pynq.io> & <https://github.com/Xilinx/PYNQ>  
<http://zedboard.org/product/ultra96>



Ultra96 PYNQ platform will be hosted on Avnet's github:

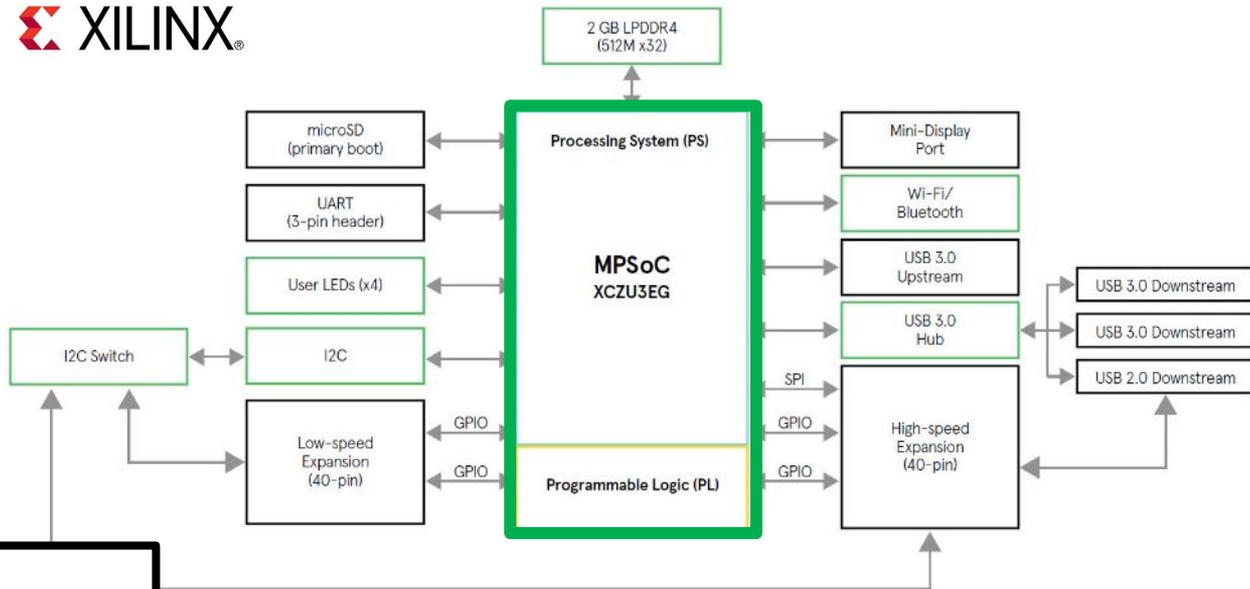
<http://github.com/Avnet>



Also come to my 2nd Linaro Connect presentation later today: “A Call to Action: Accelerating Python with FPGAs”



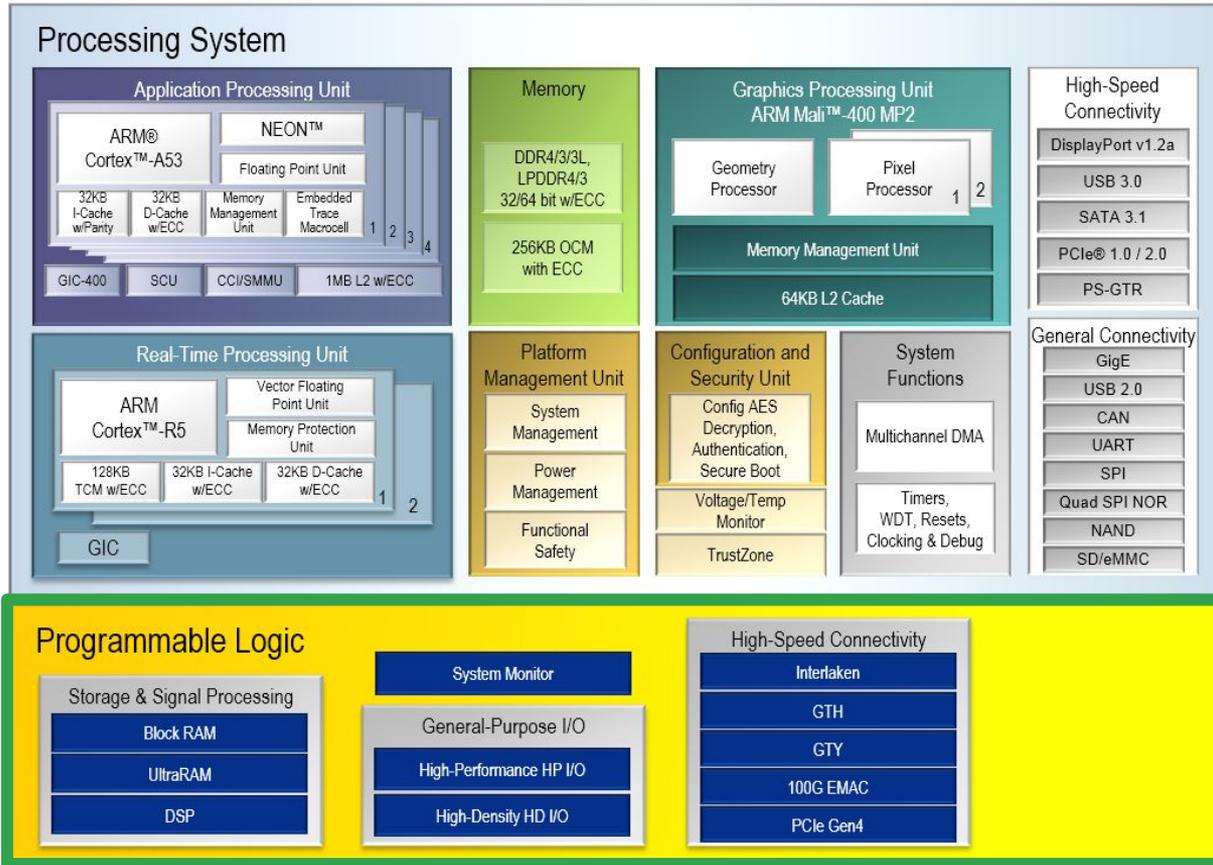
# Accelerating the search for Black Holes with Ultra96:



## Important terms:

PS = CPUs/Processing System  
PL = Programmable Logic/Hardware,  
(FPGA and some Xilinx hard IP)

# Ultra96 PS + PL all in one MPSoC ZYNQ:



## Ultra96's ZU3EG ZYNQ UltraScale+ MPSoC

**PS** = Processing System  
**PL** = Programmable Logic (FPGA)

# Compelling reasons to use the PL vs PS:

1. For many operations like convolution (time-domain filtering) and the FFT the PL will be orders of magnitude faster mainly due to parallelism and the PL's built-in DSP slices (MAC) hardware!
2. Precision timing (picoseconds of jitter accuracy) for control of other hardware
3. Determinism of algorithmic execution (no cache or interrupts if you design it that way)
4. You can program the PL to do anything, even design your own CPU/GPU. For example see Xilinx's MicroBlaze™ for PYNQ:  
[https://pynq.readthedocs.io/en/v2.0/pynq\\_libraries/pynq\\_microblaze\\_subsystem.html](https://pynq.readthedocs.io/en/v2.0/pynq_libraries/pynq_microblaze_subsystem.html)
5. The art of designing hardware with software can be rewarding and enjoyable!

Notes:

My 2<sup>nd</sup> presentation later today "A Call to Action: Accelerating Python with FPGAs" will go into more details.

# Compelling reasons to use the PL vs PS redux:

1. The PL hardware has 100's and 1000's of built-in primitives that excel at bit manipulations, modulo arithmetic, multiplication and logical operations as well as memory. Many physical I/O pins for interfacing with external hardware. All of which can be combined to accomplish just about anything.
2. The hardware can exploit true parallelism (analogous to SW threads and processes)
3. The hardware can maintain synchronous timing with small jitter in units of picoseconds
4. Because of the precise timing capabilities, reliable determinism can be designed in (in it's simplest sense you will know exactly when you will have your answer)
5. Some people enjoy the art of hardware design using software 😊

## Challenges to overcome when accelerating with hardware:

1. Identifying appropriate functionality to move into the PL
2. Moving the data between Python on the PS and the PL
3. Understanding the sensitivity of algorithms to quantization error and required mathematical precision
4. You will also need to design the hardware itself to execute the algorithms

Using the PYNQ framework will help solve some of these obstacles more quickly.

# Obstacle 1 – Identifying candidates to move into the PL

You must find the calculations that are slowing down Python and move the functionality into the PL.

A good example candidate from the LIGO Notebook: Numpy's Power Spectral Density function and FFT.

```
"mlab.psd(strain_H1, Fs = fs, NFFT = NFFT)"
```

Hints: Use your favorite Python package (cProfile, profile, hotshot, etc) and profile the code. Look at the source or use knowledge and intuition to identify code that will require a lot of mathematical computation. Look at code that is attempting to manipulate or compute in any Galois Field or doing binary bit manipulations or streaming or block operations on large amounts of data. These are typically excellent candidates! The PL can have some access to large amounts of moderately fast external memories. The PL has direct high speed access to smaller chunks of internal memories. Algorithms that require large amounts of high speed memory will be more work to move into hardware. An example of something that typically will not work well in the PL is searching and sorting large amounts of data. I don't mean impossible, rather the CPU (PS) is likely a better candidate for those tasks, it does depend on many factors.

## Obstacle 2 - Understanding mathematical precision

You must understand the sensitivity of your algorithm to quantization error and mathematical precision requirements.

Hints: Built-in Python floating point numbers are double precision with an 11-bit exponent for dynamic range and 52-bits mantissa for quantization. Numpy offers 128-bit floating point precision. PL can implement floating point arithmetic but it will generally use more resources than fixed point. Typically PL signal processing math is done with signed or unsigned fixed point integers. In some cases hybrid solutions of floating point and fixed-point are applied to compromise accuracy, speed and resource usage. Depending on the algorithm, bit for bit compatible math may or may not have a detrimental effect. This aspect can cost additional development time.

## Obstacle 3 - Moving the data between the PS and the PL

You will need to move data between the Python environment on the PS and the PL.

Hints: PYNQ can help you here! Study the PYNQ community examples. spooNN (ML CNN application) shows how to use the Python libraries for moving data with DMA. Alternatively you can use Python to C methodologies and utilize Xilinx's SDSoC tools. SDSoC allows one to write in C/C++ and through the use of proprietary compiler pragmas to convert the code into PL. SDSoC also handles moving the data between PS and PL for you. If this is your first time attempting to utilize the PL, using PYNQ is going to be easier.

# Obstacle 4 – Designing the hardware to execute the algorithm

## You will need to design the hardware that executes the algorithm

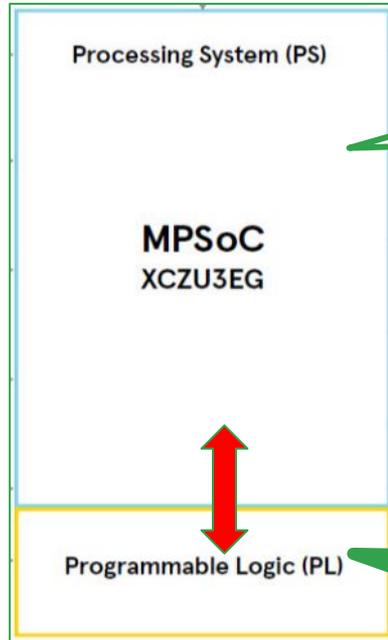
Hints: This is the largest obstacle to overcome. If you are completely new to this, you must peruse the existing PYNQ community examples and documentation. The troubles can become compounded by not having enough resources in the PL portion for more complicated algorithms. Execution speed is another practical factor that can complicate design completion. Using different larger parts that have more PL resources to allow for quicker development is not that uncommon in the industry. If you are stuck with a certain size part you may not be able to conveniently fit all of it into the PL, more effort and compromise will be required. You may have to design a hybrid system where the PS and PL each do part of the job. Due to many variables you will have to try and build it before you know whether it will work successfully; that should be considered in your schedule of work. If you are not versed in the typical hardware design languages (VHDL, Verilog), the highly recommended and superb alternatives from Xilinx for PYNQ are SDSoC and HLx. There is also an unrelated 3<sup>rd</sup> party project which allows hardware design to be accomplished with Python (see: <http://www.myhdl.org> ). One downside to MyHDL at this time is that it is not directly integrated for you into PYNQ, you would have to figure that out yourself.

Verification is another part of hardware design. For people new to the process, for complex designs this can take a significant amount of time. Using PYNQ with HLx or SDSoC helps bypass a lot of the verification steps as well. The re-use of already verified libraries and IP are what help a lot here.

As far as low-cost tools for PL design, ones that work with Ultra96, Xilinx has kindly made them available. PYNQ is free open source. For SDSoC a free voucher is included with the purchase of an Ultra96 board. There are free Webpack tools available for download after registering with Xilinx. Sign-up for free through here:

<https://www.xilinx.com/products/design-tools/software-zone.html>

# Accelerating the search for Black Holes:

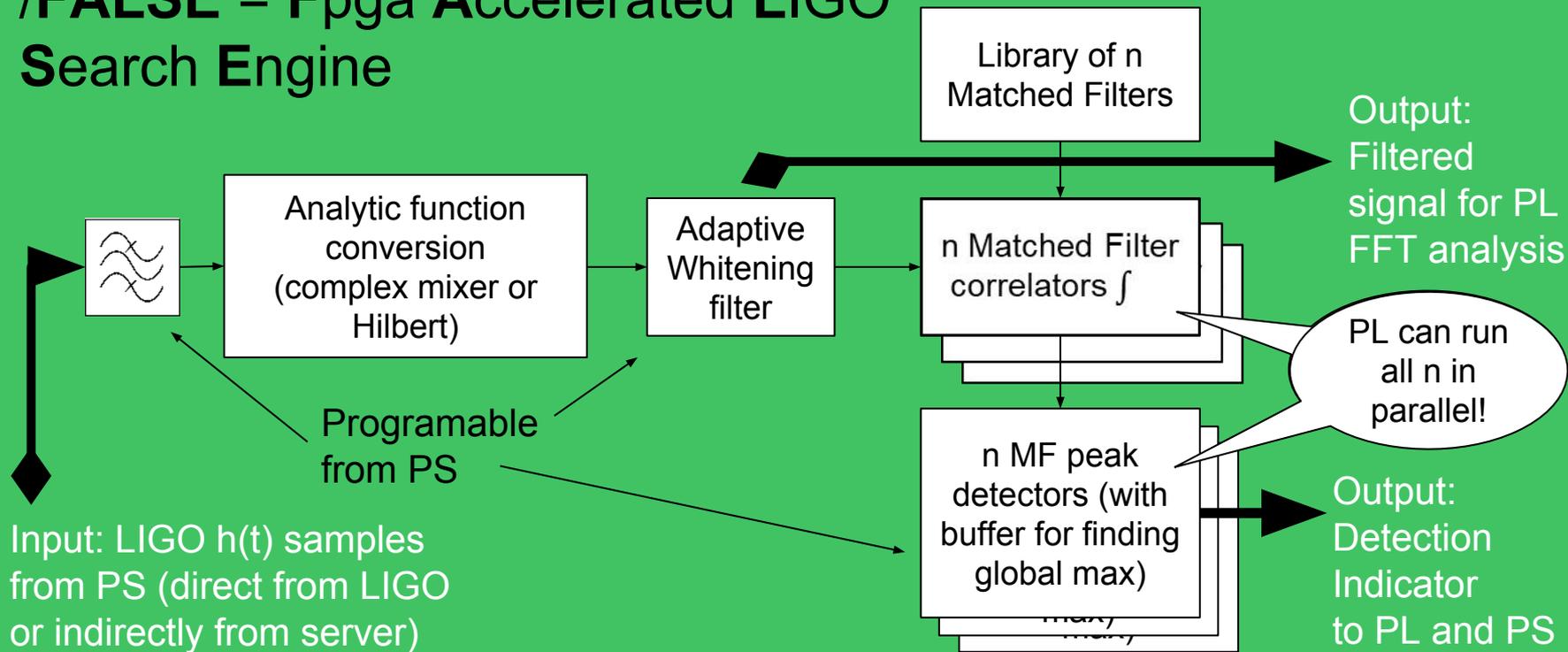


Without acceleration  
the CPUs (PS) run  
everything:  
Linux/Jupyter/Notebook  
/LIGO-search-PYTHON

Using PYNQ and various tools  
we can move the data and the  
algorithmic processing from  
the CPUs into the PL  
hardware = much faster  
execution = finding more black  
holes!

# PL LIGO processing concept design: TRUE

## /FALSE = Fpga Accelerated LIGO Search Engine



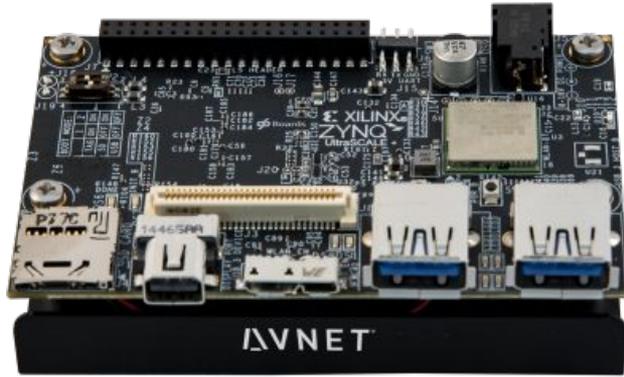
Conceptual content created by Fred Kellerman

# Acquire your own Ultra96 board for \$249:

<http://zedboard.org/product/ultra96>



**Order here**



Includes:

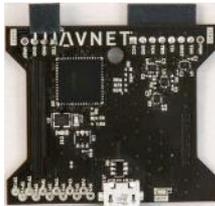
- Ultra96 development board
- 16 GB pre-loaded MicroSD card + adapter
- Voucher for SDSoc license from Xilinx
- Quick-start instruction card

Does not include (but necessary):

- External 12V 2A 96boards adapter

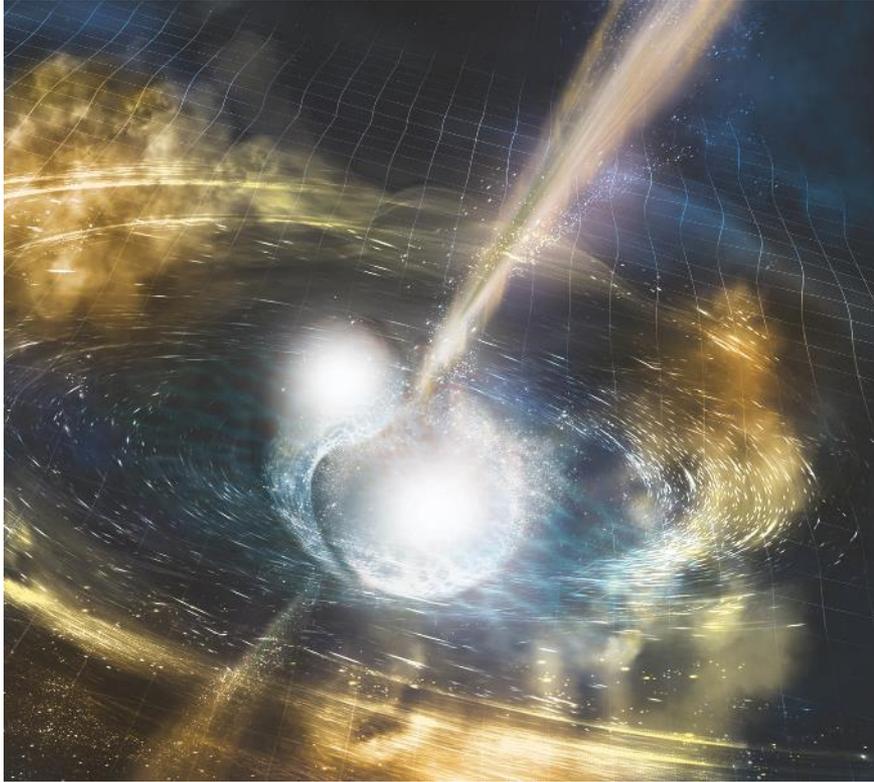
Optional Accessories:

- Seed Studios Grove Starter Kit for 96boards
- Other compatible accessories
- JTAG to USB adapter board



Further proof:

# Neutron star merger further authenticates the system!



courtesy of Caltech/MIT/LIGO Laboratory

## **GW170817**

When neutron stars merge they emit electromagnetic energy also in the visual spectrum

For this GW event, both LIGO and Virgo measured gravity waves.

Moments later the light show occurred and 70 optical telescopes directed their gaze to the area of the sky that LIGO predicted and watched the fireworks!

# Acknowledgements:

THANK YOU for attending!

Much gratitude to my friend **Aron Khan** who weathered v1.0 of my presentation and offered very useful advice to improve it

A special thank you to Dr Ofek Birnholtz PhD GW Research Scientist at RIT for personally enlightening me about this fascinating topic!

And thank you to the following people who provided for the opportunity to share this with you:

Avnet: Kevin Keryk, Bryan Fletcher

# Materials credits:

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All diagrams and information are provided as-is with no guarantee or liabilities. Any information utilized is at your own risk, none of it is intended for real-world usage, there may be many errors and flaws in this information.

Any additional diagrams, statements or imagery, unless noted were created and owned by the author.

# Get more help on PYNQ™ and Python for Ultra96:

PYNQ Workshop: [https://github.com/Xilinx/PYNQ\\_Workshop](https://github.com/Xilinx/PYNQ_Workshop)

See other's examples (Ultra96 examples will be added soon):

<http://www.pynq.io/community>

See Avnet's Ultra96 tutorials (more on the way):

<http://zedboard.org/support/design/24166/156>

Join Xilinx's Developer Zone to access free tools:

<https://www.xilinx.com/products/design-tools/software-zone.html>

Did I mention my 2<sup>nd</sup> presentation at Linaro Connect later today:

“A Call to Action: Accelerating Python with FPGAs”